

COURSE SPECIFICATION FORM

DEPARTMENT OF: Mathematics				Academic Session: 2017-18	
Course Code:	MT2900	Course Value:	0.5	Status: (ie: Core, or Optional)	Mandatory for G100, G103, G1G3, all Mathematics majors, Optional for others.
Course Title:	Complex Variable			Availability: (state which teaching terms)	Term 2
Prerequisites:	MT1710, MT1720 and MT1810			Recommended:	
Co-ordinator:					
Course Staff					
Aims:	This course is designed to provide an outline of the basic complex variable theory with some proofs. Applications are exhibited as used in other areas of mathematics. The object is to equip students to be able to use complex analysis to solve specific problems.				
Learning Outcomes:	<p>On completion of the course, the students should be able to:</p> <ul style="list-style-type: none"> • use the definitions of continuity and differentiability of a complex valued function at a point, establish the necessity of the Cauchy-Riemann equations and apply this result; • use a power series to define the complex exponential function and hence define the trigonometric and hyperbolic functions and the complex logarithm, and establish their properties; • use the parametric definition of a contour integral in specific straightforward examples; • state and use Cauchy's Theorem, and apply Cauchy's Integral Formulae to evaluate integrals; • obtain Taylor series of rational and other functions of standard type; • determine zeros and poles of given functions, and the residue at a simple pole and at higher order poles; • state Cauchy's Residue Theorem and apply it to evaluate real integrals (using Jordan's lemma when relevant) and to sum certain series, and state and use Rouché's Theorem. 				
Course Content:	<p>Special functions: Power series and radius of convergence. Discussion of the exponential, trigonometric and hyperbolic functions for both real and complex variable. Definition of $\log z$ and z^a.</p> <p>Topology: An open (pathwise) connected set of the plane.</p> <p>Functions of a complex variable: Continuity and differentiability of functions defined on an open set. The Cauchy-Riemann equations and Laplace's equation. Contour integrals along piecewise smooth curves C, defined by</p> $\int f(z)dz = \int f(z(t))z'(t)dt.$ <p>Cauchy's theorem and Cauchy's integral formulae. Taylor series with examples, removable singularities, zeros and poles. Residue theorem and applications: calculation of simple integrals, including use of Jordan's lemma, and summation of infinite series. Principle of the argument. Rouché's theorem and the location of zeros of polynomials.</p>				
Teaching & Learning Methods:	33 hours of lectures and examples classes, 117 hours of private study, including work on problem sheets and examination preparation. This may include discussions with the course leader if the student wishes.				
Key Bibliography:	Complex Analysis – J M Howie (Springer 2003). <i>Library Ref. 515.24 HOW</i> Theory and Problems of Complex Variables – M R Spiegel (Schaum 2007). <i>Library Ref. 510.76 SPI</i> Advanced Engineering Mathematics 8 th ed. – E Kreysig (Wiley 2005). <i>Library Ref. 510.245 KRE</i>				
Formative Assessment & Feedback:	Formative assignments in the form of 10 problem sheets. The students will receive feedback as written comments on their attempts.				
Summative Assessment:	Exam (%) A two-hour paper: 100% Coursework (%) None				

Updated September 2017

The information contained in this course outline is correct at the time of publication, but may be subject to change as part of the Department's policy of continuous improvement and development. Every effort will be made to notify you of any such changes.